

# Smallness of neutrino mass from trans-Planckian asymptotic safety

**Enrico Maria Sessolo**

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in collaboration with

Kamila Kowalska and Soumita Pramanick

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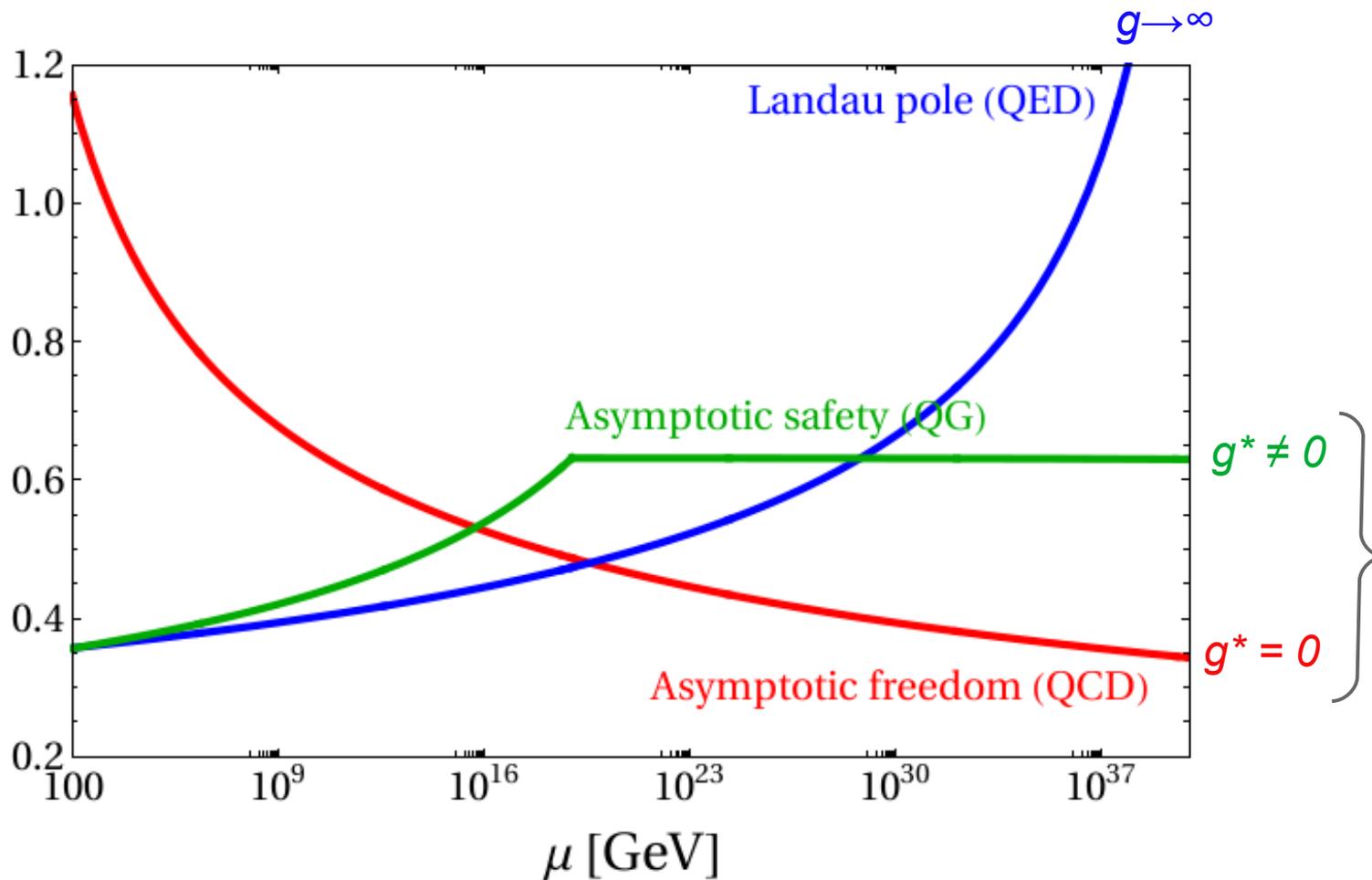
**SONATA BIS 10** (PI: E.M.Sessolo)  
**SONATA BIS 7** (PI: K. Kowalska)



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# Renormalization group flow

Charge-screening by quantum fluctuations  $\rightarrow$  *running* coupling constants,  $g_i(\mu)$



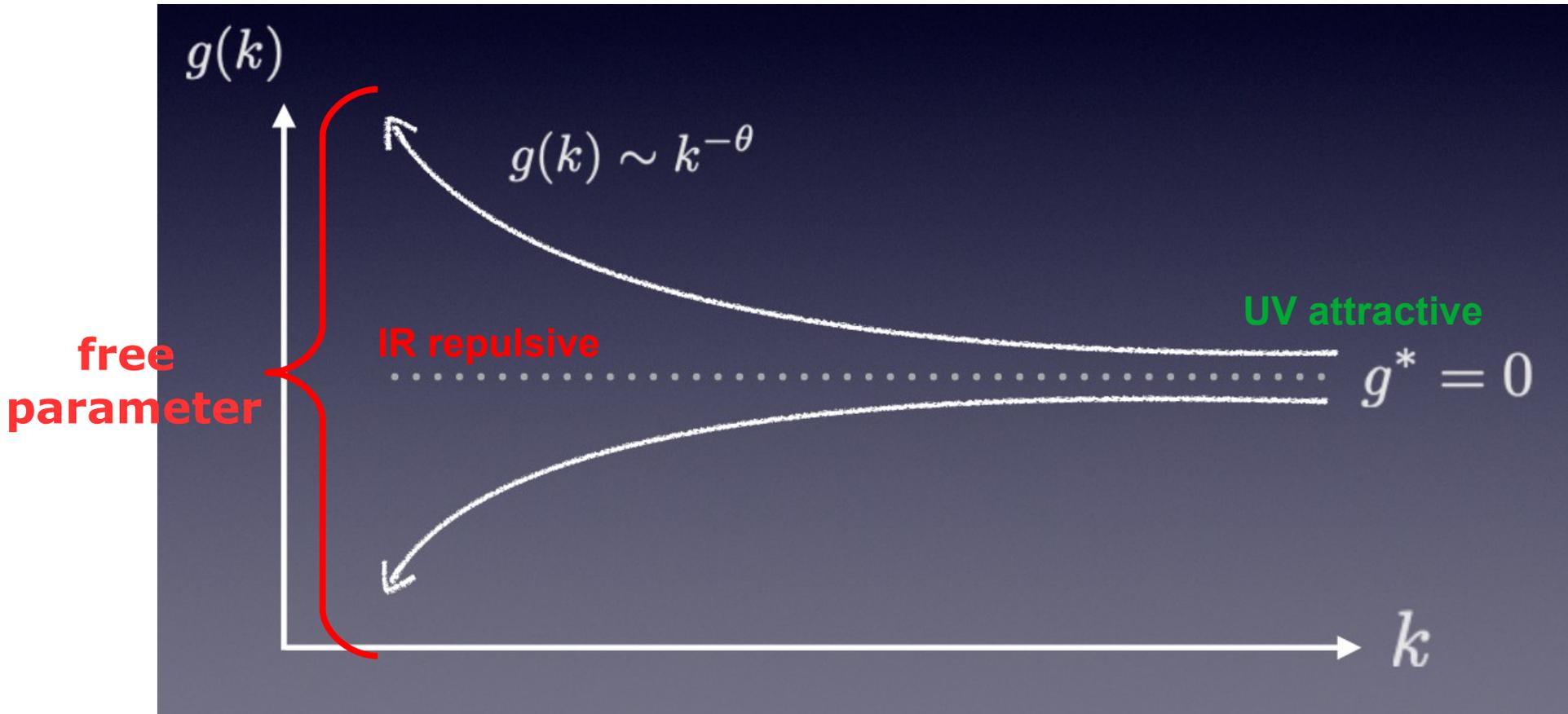
$$\beta_g = \frac{dg}{dt} = \frac{dg}{d \ln \mu}$$

$$\beta_g(g^*) = 0$$

**fixed point  $g^*$   
in the RG flow**

# Scaling properties of $g_i$

critical exponent  $\theta > 0$

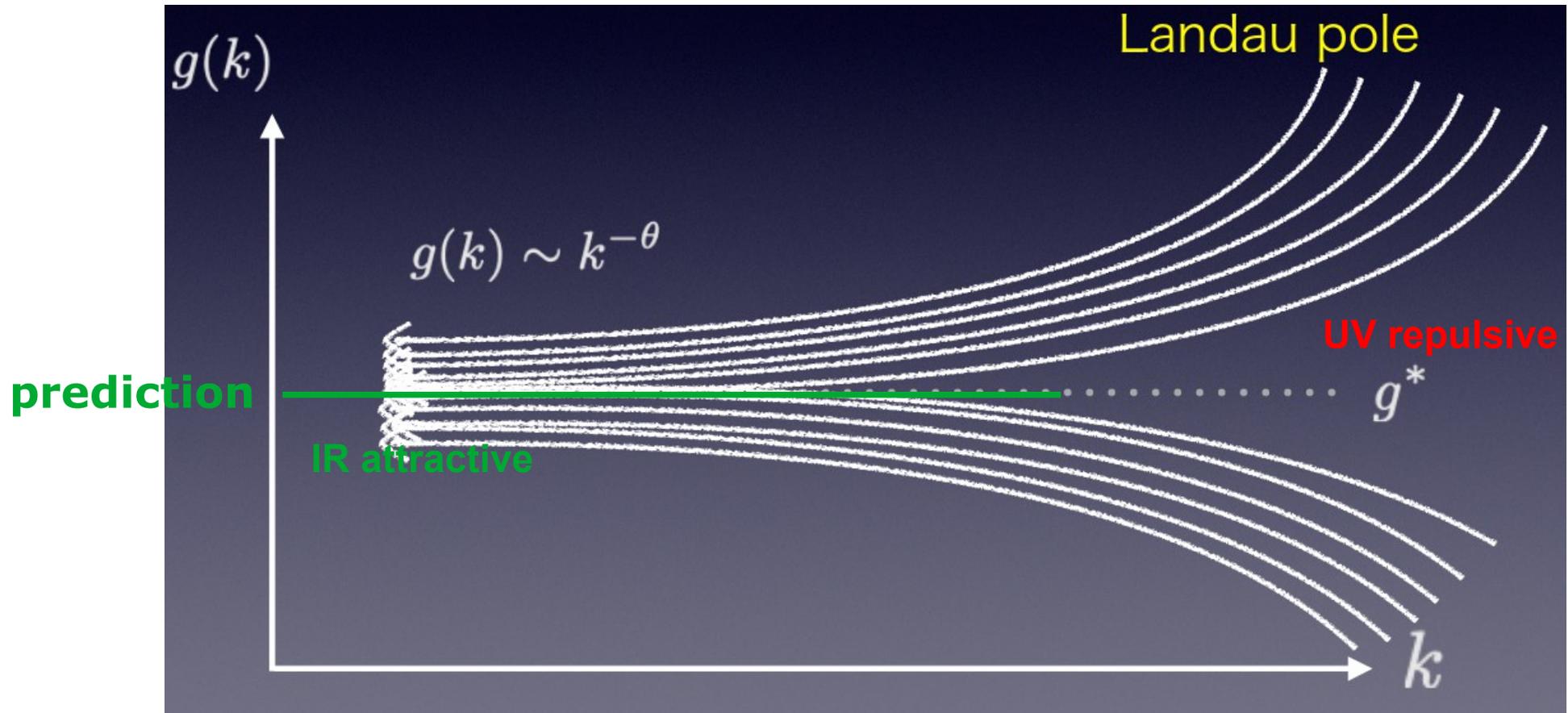


M.Yamada, HECA seminar, 08.10.2019

**Relevant** couplings are **free parameters**

# Scaling properties of $g_i$

critical exponent  $\theta < 0$



M.Yamada, HECA seminar, 08.10.2019

**Irrelevant** couplings provide **predictions**

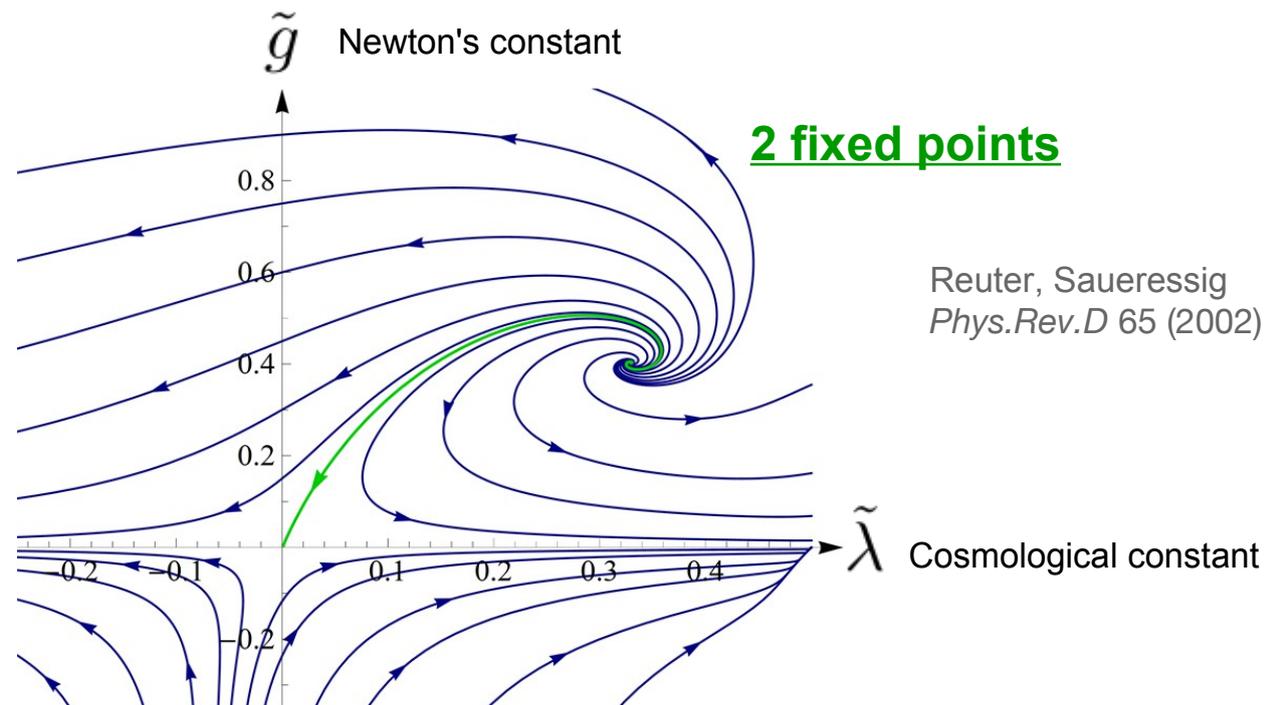
# QFTs with fixed points

## Quantum gravity might feature interactive UV fixed points (functional renormalization group)

Reuter '96, Reuter, Saueressig '01, Litim '04, Codello, Percacci, Rahmede '06, Benedetti, Machado, Saueressig '09, Narain, Percacci '09, Manrique, Rechenberger, Saueressig '11, Falls, Litim, Nikolakopoulos '13, Dona', Eichhorn, Percacci '13, Daum, Harst, Reuter '09, Folkerst, Litim, Pawłowski '11, Harst, Reuter '11, Zanusso *et al.* '09 ... many more

$$\Gamma_k = -\frac{1}{16\pi G_N} \int d^4x \sqrt{g} (R - 2\bar{\Lambda}) \quad \tilde{g} = G_N k^2, \quad \tilde{\lambda} = \bar{\Lambda} k^{-2}$$

scale dependence



# QFTs with fixed points

## Quantum gravity plus matter

Christiansen, Eichhorn '17, Christiansen *et al.* '17, Shaposhnikov, Wetterich '09, Oda, Yamada '15, Eichhorn, Held, Pawłowski '16, Wetterich, Yamada '16, Hamada, Yamada '17, Pawłowski *et al.* '18, Eichhorn, Versteegen '17, Eichhorn, Held '17-'18 ...

Beta functions of the SM:

hypercharge

$$\frac{dg_Y}{dt} = \frac{g_Y^3}{16\pi^2} \frac{41}{6}$$

weak

$$\frac{dg_2}{dt} = -\frac{g_2^3}{16\pi^2} \frac{19}{6}$$

strong

$$\frac{dg_3}{dt} = -\frac{g_3^3}{16\pi^2} 7$$

Yukawa couplings

$$\frac{dy_t}{dt} = \frac{y_t}{16\pi^2} \left( \frac{9}{2}y_t^2 + \frac{3}{2}y_b^2 + 3y_s^2 + 3y_c^2 - \frac{9}{4}g_2^2 - 8g_3^2 - \frac{17}{12}g_Y^2 + y_e^2 + y_\mu^2 + y_\tau^2 \right)$$

$$\frac{dy_b}{dt} = \frac{y_b}{16\pi^2} \left( \frac{9}{2}y_b^2 + \frac{3}{2}y_t^2 + 3y_s^2 + 3y_c^2 - \frac{9}{4}g_2^2 - 8g_3^2 - \frac{5}{12}g_Y^2 + y_e^2 + y_\mu^2 + y_\tau^2 \right)$$

.... other quarks and leptons ...

# QFTs with fixed points

## Quantum gravity plus matter

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### Correction due to strong gravity:

hypercharge

$$\frac{dg_Y}{dt} = \frac{g_Y^3}{16\pi^2} \frac{41}{6} - f_g g_Y$$

weak

$$\frac{dg_2}{dt} = -\frac{g_2^3}{16\pi^2} \frac{19}{6} - f_g g_2$$

strong

$$\frac{dg_3}{dt} = -\frac{g_3^3}{16\pi^2} 7 - f_g g_3$$

Yukawa couplings

$$\frac{dy_t}{dt} = \frac{y_t}{16\pi^2} \left( \frac{9}{2}y_t^2 + \frac{3}{2}y_b^2 + 3y_s^2 + 3y_c^2 - \frac{9}{4}g_2^2 - 8g_3^2 - \frac{17}{12}g_Y^2 + y_e^2 + y_\mu^2 + y_\tau^2 \right) - f_y y_t$$

$$\frac{dy_b}{dt} = \frac{y_b}{16\pi^2} \left( \frac{9}{2}y_b^2 + \frac{3}{2}y_t^2 + 3y_s^2 + 3y_c^2 - \frac{9}{4}g_2^2 - 8g_3^2 - \frac{5}{12}g_Y^2 + y_e^2 + y_\mu^2 + y_\tau^2 \right) - f_y y_b$$

.... other quarks and leptons ...

$$f_g = \tilde{g} \frac{1 - 4\tilde{\lambda}}{4\pi(1 - 2\tilde{\lambda})^2}$$

$$f_y = \frac{96 + \tilde{\lambda}[-235 + \tilde{\lambda}(103 + 56\tilde{\lambda})]}{12\pi[3 + 2\tilde{\lambda}(-5 + 4\tilde{\lambda})]^2} \tilde{g}$$

# QFTs with fixed points

## Quantum gravity plus matter

Christiansen, Eichhorn '17, Christiansen *et al.* '17, Shaposhnikov, Wetterich '09, Oda, Yamada '15, Eichhorn, Held, Pawłowski '16, Wetterich, Yamada '16, Hamada, Yamada '17, Pawłowski *et al.* '18, Eichhorn, Versteegen '17, Eichhorn, Held '17-'18 ...

### Find the zeroes ...

hypercharge

$$\frac{dg_Y}{dt} = \frac{g_Y^3}{16\pi^2} \frac{41}{6} - f_g g_Y = 0$$

weak

$$\frac{dg_2}{dt} = -\frac{g_2^3}{16\pi^2} \frac{19}{6} - f_g g_2 = 0$$

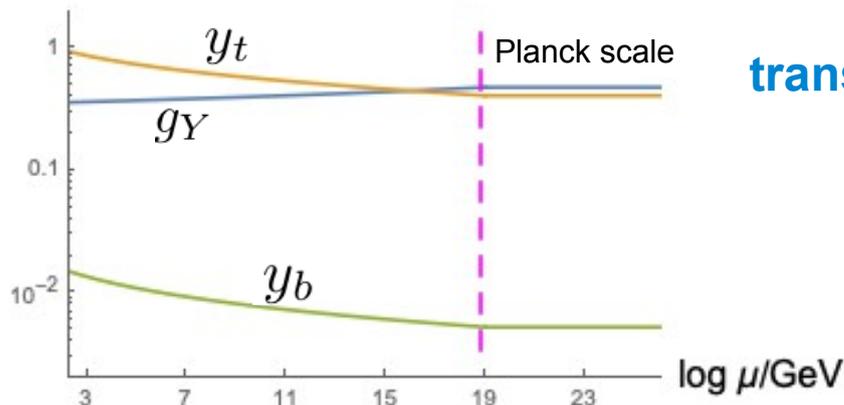
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$$\frac{dg_3}{dt} = -\frac{g_3^3}{16\pi^2} 7 - f_g g_3 = 0$$

Yukawa couplings

$$\frac{dy_t}{dt} = \frac{y_t}{16\pi^2} \left( \frac{9}{2}y_t^2 + \frac{3}{2}y_b^2 + 3y_s^2 + 3y_c^2 - \frac{9}{4}g_2^2 - 8g_3^2 - \frac{17}{12}g_Y^2 + y_e^2 + y_\mu^2 + y_\tau^2 \right) - f_y y_t = 0$$

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trans-Planckian fixed points of matter!

# Comments ...

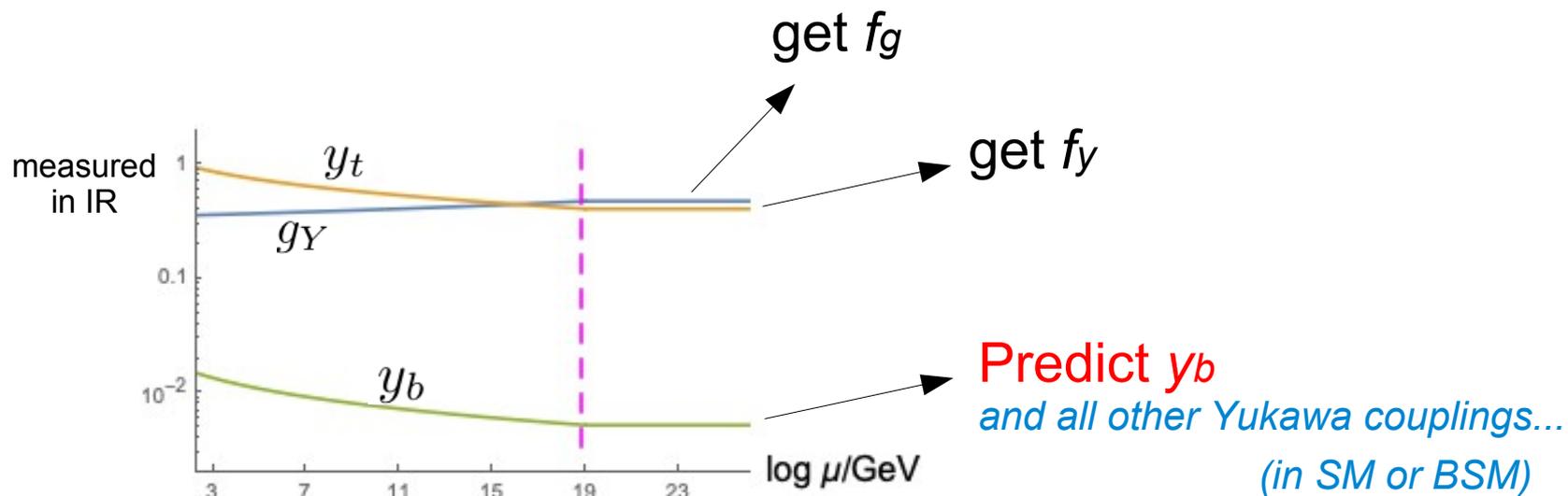
- **FRG calculation of  $f_g, f_y$  has very large uncertainties...** (truncation in number of operators, cut-off scheme dependence, etc.)

Lauscher, Reuter '02, Codello, Percacci, Rahmede '07-'08, Benedetti, Machado, Saueressig '09, Narain, Percacci '09, Dona', Eichhorn, Percacci '13, Falls, Litim, Schroeder '18 ...

- **FRG calculation is not required to get predictions...**

Wetterich, Shaposhnikov '09, Eichhorn, Held '18, Reichert, Smirnov '19; Alkofer *et al.* '20, Kowalska, EMS, Yamamoto '20, Kowalska, EMS '21, Chikkaballi, Kotlarski, Kowalska, Rizzo, EMS '22 ...

... as the set of *irrelevant* couplings is overconstrained: 3 eqs ( $g_Y, y_t, y_b$ )  
2 unknowns ( $f_g, f_y$ )



# Neutrinos

Neutrino masses are very small !

NuFIT5.1 (2021) 2007.14792

Planck (2021) 1807.06209

$$\Delta m_{21}^2 = 7.42_{-0.20}^{+0.21} \times 10^{-5} \text{ eV}^2,$$

$$\text{NO: } \Delta m_{31}^2 = 2.515_{-0.028}^{+0.028} \times 10^{-3} \text{ eV}^2,$$

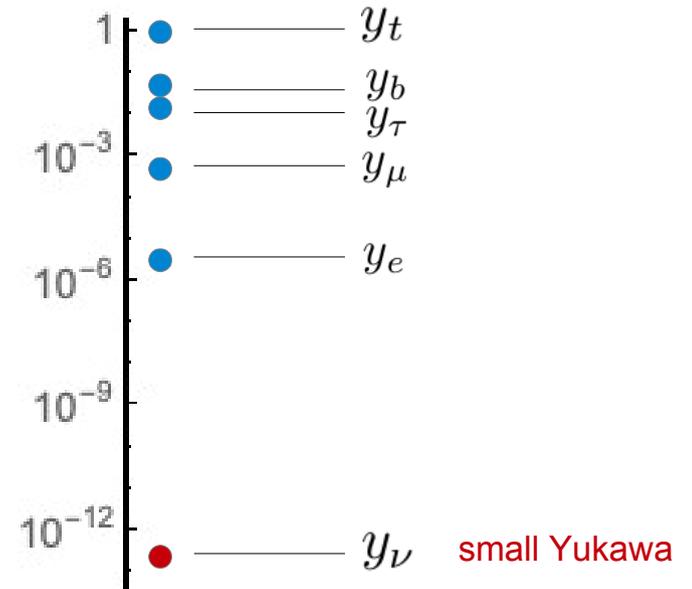
$$\text{IO: } \Delta m_{32}^2 = -2.498_{-0.029}^{+0.028} \times 10^{-3} \text{ eV}^2,$$

$$\sum_{i=1,2,3} m_i < 0.12 \text{ eV}$$

... either Dirac neutrino ...

New Yukawa → Higgs mechanism:

$$\mathcal{L}_D = -y_\nu^{ij} \nu_{R,i} (H^c)^\dagger L_j + \text{H.c.}$$



# Neutrinos

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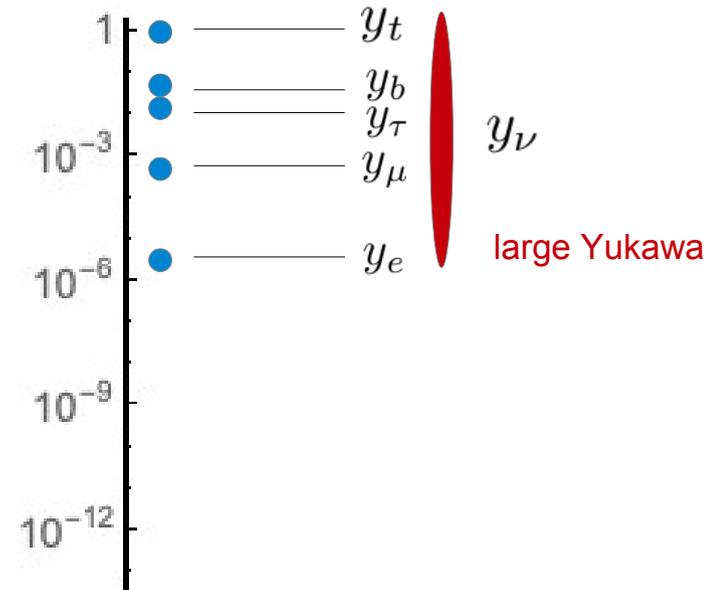
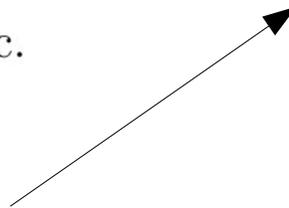
$$\sum_{i=1,2,3} m_i < 0.12 \text{ eV}$$

.... or Majorana neutrino

see-saw mechanism:

$$\mathcal{L}_M = \mathcal{L}_D - \frac{1}{2} M_N^{ij} \nu_{R,i} \nu_{R,j} + \text{H.c.}$$

$$m_\nu \approx \frac{y_\nu^2 v_h^2}{\sqrt{2} M_N}$$



# What is predicted?

## Fixed-point analysis:

$$\begin{aligned}\frac{dg_Y}{dt} &= \frac{g_Y^3}{16\pi^2} \frac{41}{6} - f_g g_Y = 0 && \longrightarrow \text{get } f_g \\ \frac{dy_t}{dt} &= \frac{y_t}{16\pi^2} \left[ \frac{9}{2} y_t^2 + y_\nu^2 - \frac{17}{12} g_Y^2 \right] - f_y y_t = 0 && \longrightarrow \text{get } f_y \\ \frac{dy_\nu}{dt} &= \frac{y_\nu}{16\pi^2} \left[ 3y_t^2 + \frac{5}{2} y_\nu^2 - \frac{3}{4} g_Y^2 \right] - f_y y_\nu = 0 && \longrightarrow \text{Predict } y_\nu\end{aligned}$$

Two *irrelevant* solutions for the neutrino fixed point:

1.  $y_\nu^{*2} = \frac{32\pi^2}{5} f_y + \frac{3}{10} g_Y^{*2} - \frac{6}{5} y_t^{*2}$  (interactive)

2.  $y_\nu^* = 0$  (Gaussian)

# What is predicted?

## Fixed-point analysis:

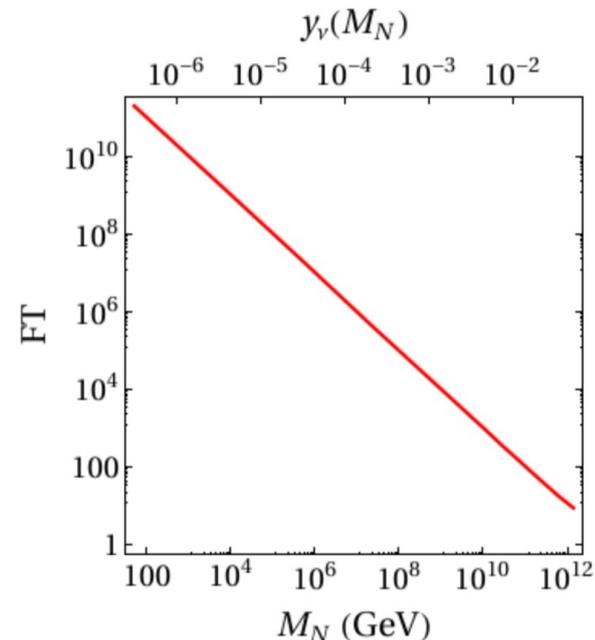
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Two *irrelevant* solutions for the neutrino fixed point:

$$1. \quad y_\nu^{*2} = \frac{32\pi^2}{5} f_y + \frac{3}{10} g_Y^{*2} - \frac{6}{5} y_t^{*2}$$

large fine tuning of  $f_y$  to get small Yukawa

→ perhaps neutrino is Majorana?

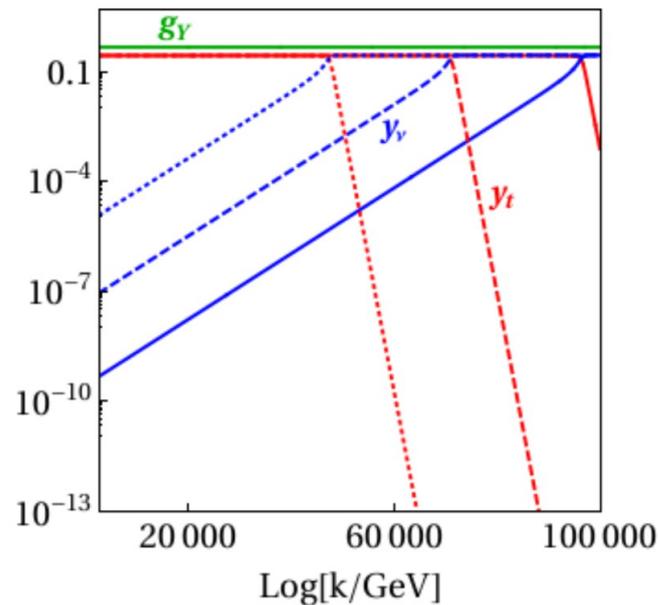
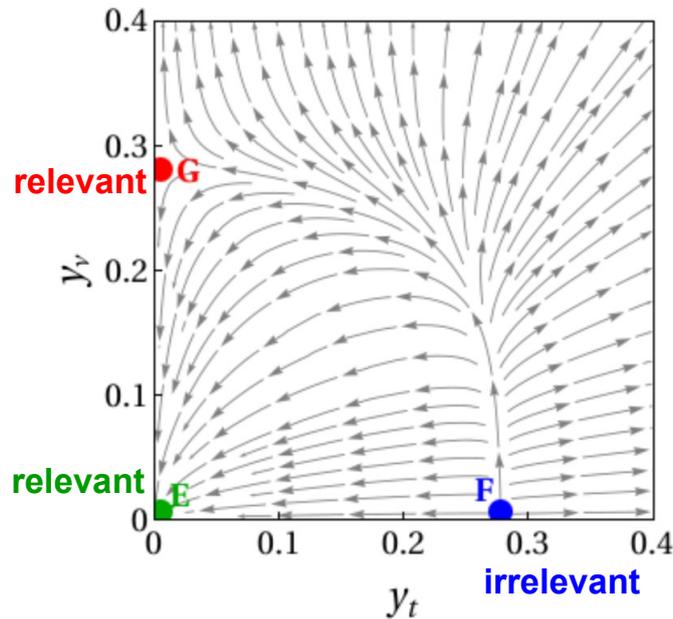


# What is predicted?

2.  $y_\nu^* = 0$  (irrelevant)

... then zero Yukawa coupling is predicted?

Nope (surprise!) ... **the system admits relevant fixed points too!**



$$y_\nu(t; \kappa) \approx \left( \frac{16\pi^2 f_y}{e^{f_y(\kappa-t)} + 5/2} \right)^{1/2}$$

**a novel dynamical mechanism** (alternative to see-saw)

... smallness of neutrino Yukawa related to the distance of Planck scale from “infinity”

# More findings...

K.Kowalska, S.Pramanick, EMS  
*JHEP* 08 (2022) 262

- Applies uniquely to neutrino Yukawa coupling (  $\sim$  quantum singlet)
- This dynamical mechanism stands under the full set of SM RGEs
- It is easily applicable to BSM feebly interacting particles (freeze-in dark matter, pseudo-Dirac neutrinos, ALPs, etc.)